

# Direct Mining of Discriminative Patterns for Classifying Uncertain Data

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# Classification on Certain Data

## Example:

A toy example about certain categorical dataset containing 4 classes.

Evaluation	Price	Looking	Tech. Spec.	Quality
Unacceptable	+	-	/	-
Acceptable	/	-	/	/
Good	-	+	/	/
Very Good	/	+	+	+

(+: Good, /: Medium, -: Bad)

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- ▶ Train a classifier using the feature data converted from training data.

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- ▶ Different feature types - Binary, Numeric (New, NDPMine)



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A toy example about uncertain categorical dataset. The uncertainty usually is caused by noise, measurement precisions, etc.

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- ▶ Uncertain Rule-based Classifier - Ripper-based uRule

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A new associative classification algorithm working on uncertain data.

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- ▶ How to represent discriminative information?
- ▶ How to cover instances?



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### Definition of Expected Confidence:

Given a set of transactions  $T$  and the set of possible worlds  $W$  w.r.t.  $T$ , the expected confidence of an itemset  $x$  on class  $c$  is

$$E(\text{conf}_x^c) = \sum_{w_i \in W} \text{conf}_{x,w_i}^c \times P(w_i) = \sum_{w_i \in W} \frac{\text{sup}_{x,w_i}^c}{\text{sup}_{x,w_i}} \times P(w_i)$$

where  $P(w_i)$  is the probability of world  $w_i$ .  $\text{conf}_{x,w_i}^c$  is the respected confidence of  $x$  on class  $c$  in world  $w_i$ , while  $\text{sup}_{x,w_i}$  ( $\text{sup}_{x,w_i}^c$ ) is the respected support of  $x$  (on class  $c$ ) in world  $w_i$ .

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$O(\prod_{A_k \in \mathbb{A}^u} |\text{dom}_{A_k}|^{|T|})$  possible worlds.

# Efficient Computation of Expected Confidence

Lemma:

Since  $0 \leq \text{sup}_x^c \leq \text{sup}_x \leq |T|$ , we have:

$$\begin{aligned} E(\text{conf}_x^c) &= \sum_{w_i \in W} \text{conf}_{x, w_i}^c \times P(w_i) \\ &= \sum_{i=0}^{|T|} \sum_{j=0}^i \frac{j}{i} \times P(\text{sup}_x = i \wedge \text{sup}_x^c = j) \\ &= \sum_{i=0}^{|T|} \frac{E_i(\text{sup}_x^c)}{i} = \sum_{i=0}^{|T|} E_i(\text{conf}_x^c) \end{aligned}$$

, where  $E_i(\text{sup}_x^c)$  and  $E_i(\text{conf}_x^c)$  denote the part of expected support and confidence of itemset  $x$  on class  $c$  when  $\text{sup}_x = i$ .

## Efficient Computation of Expected Confidence

Given  $0 \leq n \leq |T|$ , define  $E_n(\text{sup}_x^c) = \sum_{i=0}^{|T|} E_{i,n}(\text{sup}_x^c)$  as the expected support of  $x$  on class  $c$  on the first  $n$  transactions of  $T$ , and  $E_{i,n}(\text{sup}_x^c)$  as the expected support of  $x$  on class  $c$  with support of  $i$  on the first  $n$  transactions of  $T$ .

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Denoting  $P(x \subseteq t_i)$  as  $p_i$  for each transaction  $t_i \in T$ , we have

$$\begin{aligned} E_{i,n}(\text{sup}_x^c) &= p_n \times E_{i-1,n-1}(\text{sup}_x^c) \\ &\quad + (1 - p_n) \times E_{i,n-1}(\text{sup}_x^c) \end{aligned}$$

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$$E_{i,n}(\text{sup}_x^c) = p_n \times E_{i-1,n-1}(\text{sup}_x^c + 1) + (1 - p_n) \times E_{i,n-1}(\text{sup}_x^c)$$

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when  $c_n = c$ , where  $1 \leq i \leq n \leq |T|$ .

$$E_{i,n}(\text{sup}_x^c) = 0$$

for  $\forall n$  where  $i = 0$ , or where  $n < i$ .



## Efficient Computation of Expected Confidence

Defining  $P_{i,n}$  as the probability of  $x$  having support of  $i$  on the first  $n$  transactions of  $T$ , we have

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when  $c_n = c$ , since we have:

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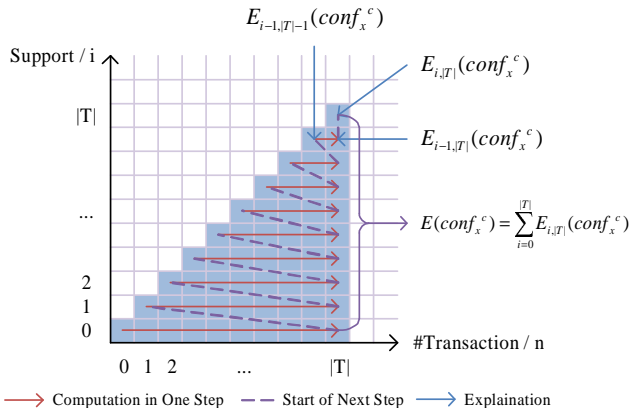
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## Efficient Computation of Expected Confidence

Since  $E(\text{conf}_x^c) = E_{|T|}(\text{conf}_x^c) = \sum_{i=0}^{|T|} E_{i,|T|}(\text{conf}_x^c)$ . The computation is divided into  $|T| + 1$  steps with  $E_{i,|T|}(\text{conf}_x^c) = E_{i,|T|}(\text{sup}_x^c)/i$  ( $0 \leq i \leq |T|$ ) computed in  $i$ th step.

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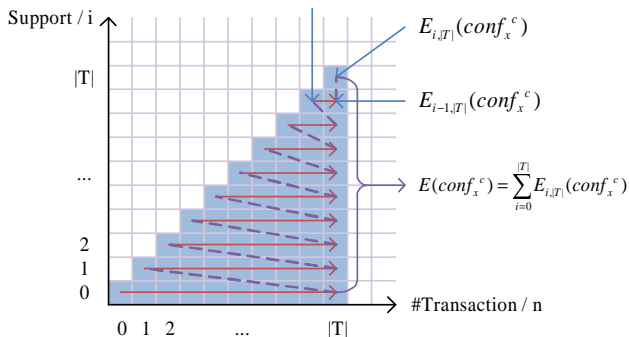
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$$E_{i-1,|T|-1}(\text{conf}_x^c)$$



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 $O(|T|^2)$

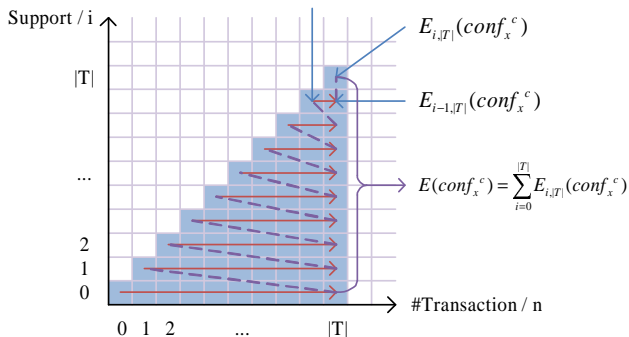
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Time Complexity:

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Space Complexity:

$$O(|T|)$$

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## Upper Bounds of Expected Confidence

For  $\forall i(1 \leq i \leq |T|)$ , we have

$$\begin{aligned} E(\text{conf}_x^c) &= E_{|T|}(\text{conf}_x^c) \\ &= \sum_{k=0}^{i-1} \frac{E_{k,|T|}(\text{sup}_x^c)}{k} + \sum_{k=i}^{|T|} \frac{E_{k,|T|}(\text{sup}_x^c)}{k} \\ &\leq \sum_{k=0}^{i-1} \frac{E_{k,|T|}(\text{sup}_x^c)}{k} + \sum_{k=i}^{|T|} \frac{E_{k,|T|}(\text{sup}_x^c)}{i} \\ &= \sum_{k=0}^{i-1} \frac{E_{k,|T|}(\text{sup}_x^c)}{k} + \sum_{k=0}^{|T|} \frac{E_{k,|T|}(\text{sup}_x^c)}{i} - \sum_{k=0}^{i-1} \frac{E_{k,|T|}(\text{sup}_x^c)}{i} \\ &= \sum_{k=0}^{i-1} E_{k,|T|}(\text{sup}_x^c) \times \left(\frac{1}{k} - \frac{1}{i}\right) + \frac{E(\text{sup}_x^c)}{i} \\ &= \text{bound}_i(\text{conf}_x^c) \end{aligned}$$

# Upper Bounds of Expected Confidence

For  $1 \leq i \leq |T|$ , we have:

$$\begin{aligned} E(\sup_x^c) &= \text{bound}_1(\text{conf}_x^c) \\ &\geq \dots \geq \text{bound}_i(\text{conf}_x^c) \geq \dots \\ &\geq \text{bound}_{|T|}(\text{conf}_x^c) = E(\text{conf}_x^c) \end{aligned}$$

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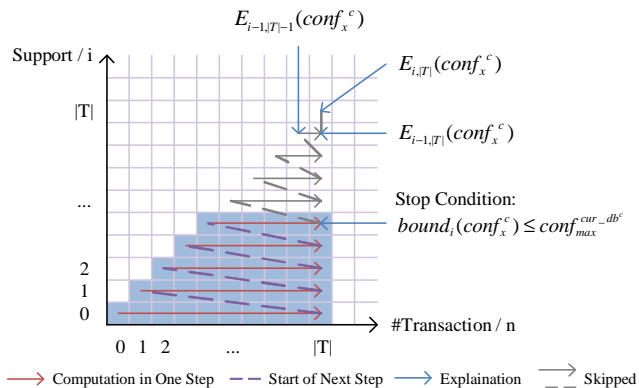
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Since

$$\begin{aligned} \text{bound}_i(\text{conf}_x^c) &= \text{bound}_{i-1}(\text{conf}_x^c) \\ &\quad - \left(\frac{1}{i-1} - \frac{1}{i}\right) \times \left(E(\sup_x^c) - \sum_{k=0}^{i-1} E_{k,|T|}(\sup_x^c)\right) \end{aligned}$$

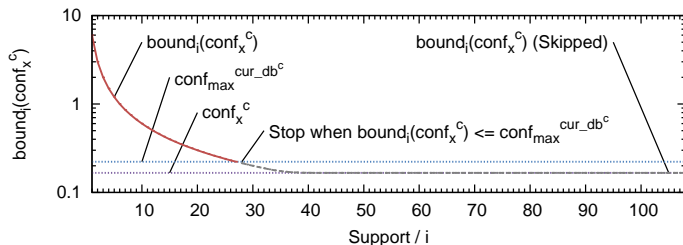
, can compute  $\text{bound}_i(\text{conf}_x^c)$  with  $\text{bound}_{i-1}(\text{conf}_x^c)$ .

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## Running Example:



# Algorithm Framework

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Need to sort all the uncertain attributes after certain attributes, to help shrink current projected database.

# Instance Covering Strategy

## Previous Strategy in HARMONY:

Just find one most discriminative covering pattern with the highest confidence for each instance. On uncertain data, the probability of the instance being covered could be very low.

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## Previous Strategy in HARMONY:

Just find one most discriminative covering pattern with the highest confidence for each instance. On uncertain data, the probability of the instance being covered could be very low.

## Our method:

Apply a threshold of minimum cover probability  $coverProb_{min}$ . Assure that the probability of each instance not covered by any pattern is less than  $1 - coverProb_{min}$ , by maintaining a list storing confidence values of covering patterns on class  $c$  in descending order.

# Used Classifiers

## SVM Classifier

Convert each pattern to a binary feature by whether it is contained by the instance.

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### Rule-based Classifier (From HARMONY)

For each test instance we just sum up the product of the confidence of each pattern on each class and the probability of the instance containing the pattern. The class with the largest value is the predicted class of the instance.

# Used Datasets

Dataset	#Instance	#Attribute	#Class	Area
australian	690	14	2	Financial
balance	635	4	3	Social
bands	539	38	2	Physical
breast	699	9	2	Life
bridges-v1	106	11	6	N/A
bridges-v2	106	10	6	N/A
car	1728	6	4	N/A
contraceptive	1473	9	3	Life
credit	690	15	2	Financial
echocardiogram	131	12	2	Life
flag	194	28	8	N/A
german	1000	19	2	Financial
heart	920	13	5	Life
hepatitis	155	19	2	Life
horse	368	27	2	Life
monks-1	556	6	2	N/A
monks-2	601	6	2	N/A
monks-3	554	6	2	N/A
mushroom	8124	22	2	Life
pima	768	8	2	Life
postoperative	90	8	3	Life
promoters	106	57	2	Life
spect	267	22	2	Life
survival	306	3	2	Life
ta_eval	151	5	3	N/A
tic-tac-toe	958	9	2	Game
vehicle	846	18	4	N/A
voting	435	16	2	Social
wine	178	13	3	Physical
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30 Public UCI Certain  
Datasets



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30 Public UCI Certain Datasets

Real values have been discretized.

# Convert to Uncertain Datasets

Two parameters:

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Represented by  $U_x@y$ , where  $x$  is uncertain degree and  $y$  is uncertain attribute number.

## Accuracy Evaluation

Average accuracies on 30 datasets. For accuracy on each dataset, refer to our paper.

### Using SVM Classifier:

Dataset	uHARMONY	DTU	uRule
U10@1	<b>79.0138</b>	74.8738	75.2111
U10@2	<b>78.6970</b>	73.1629	73.4107
U10@4	<b>77.9657</b>	72.2670	69.4649
U20@1	<b>78.9537</b>	74.6577	74.6287
U20@2	<b>78.6073</b>	72.5642	72.5460
U20@4	<b>77.8352</b>	69.9157	68.2066

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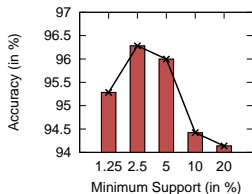
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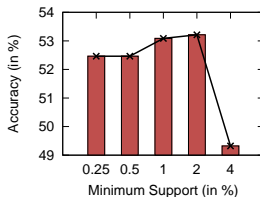
### Using Rule-based Classifier:

Dataset	uHARMONY <sup>rule</sup>	DTU	uRule
U10@4	<b>73.2517</b>	72.2670	69.4649

# Sensitivity Test



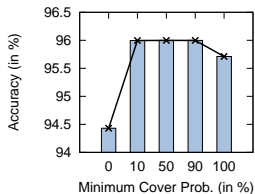
(a) breast



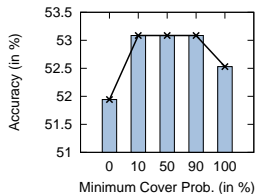
(b) wine

Figure: Accuracy Evaluation of U10@1 w.r.t. Minimum Support

# Sensitivity Test



(a) breast

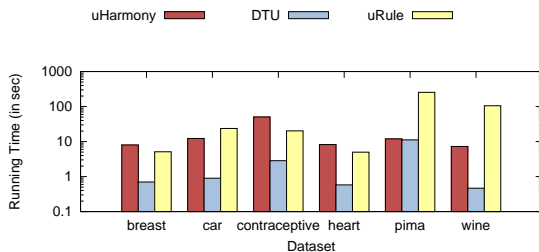


(b) wine

Figure: Accuracy Evaluation of U10@1 w.r.t. Minimum Cover Prob.



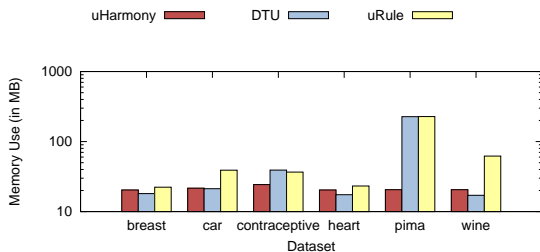
# Runtime Efficiency



(a) Running Time (in sec)

Figure: Classification Efficiency Evaluation of U10@1

# Runtime Efficiency



(b) Memory Use (in MB)

Figure: Classification Efficiency Evaluation of U10@1

# Effectiveness of the Expected Confidence Upper Bound

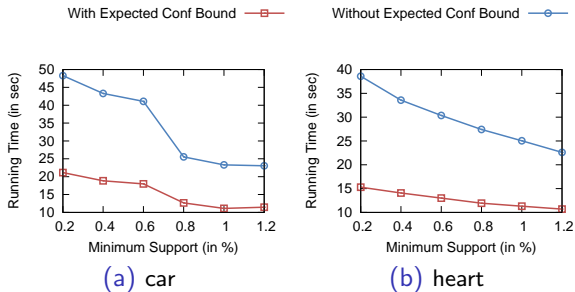
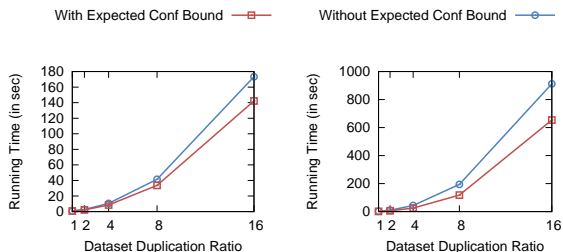


Figure: Running Time Evaluation of U10@4

# Scalability Test



(a) car ( $sup_{min} = 0.01$ )

(b) heart ( $sup_{min} = 0.01$ )

Figure: Scalability Evaluation (U10@1, Running Time)

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- ▶ Conducted an extensive evaluation on 30 public real data, under varying uncertain parameters. With significant improvements on accuracy, comparing with two other state-of-the-art algorithms.
- ▶ Evaluated the runtime efficiency, proved the effectiveness of using upper bounds.

# The End

Thank you for Listening!

## Questions or Comments?